

High-Accuracy Camera Calibration and Scene Acquisition

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Unconstrained
Imaging Model

Calibration

Rays interpolation

Central + Model-free
distortion

Flow and
Dichromatic
model recovery

Problem formulation

TV regularizer

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Presentation Outline

▶ Unconstrained imaging model

▶ Calibration



FILIPPO BERGAMASCO, ANDREA ALBARELLI, EMANUELE RODOLA, ANDREA TORSELLO

Can a Fully Unconstrained Imaging Model Be Applied Effectively to Central Cameras?

IEEE Conference on Computer Vision and Pattern Recognition, IEEE, pp. 1391-1398, CVPR, 2013.

▶ Rays interpolation



ANDREA ALBARELLI, COSMO LUCA, FILIPPO BERGAMASCO, ANDREA TORSELLO

High-Coverage 3D Scanning through Online Structured Light Calibration
22nd International Conference on Pattern Recognition, pp.4080-4085, ICPR, 2014.

▶ Central model with unconstrained distortion



FILIPPO BERGAMASCO, LUCA COSMO, ANDREA GASPARETTO, ANDREA ALBARELLI, ANDREA TORSELLO

Non-Parametric Lens Distortion Estimation for Central Cameras
UNDER REVIEW, CVPR, 2015.

▶ Simultaneous Flow and Dichromatic model recovery



FILIPPO BERGAMASCO, ANTONIO ROBLES-KELLY, ANDREA TORSELLO

Dichromatic Parameter Recovery from Two Views via Total Variation Hyper-priors
UNDER REVIEW, CVPR, 2015.



Additional topics covered in the thesis

► Fiducial markers



FILIPPO BERGAMASCO, ANDREA ALBARELLI, ANDREA TORSELLO

Pi-Tag: a fast image-space marker design based on projective invariants

Machine Vision and Applications (ISSN:0932-8092), pp. 1295- 1310, MVA, 2013.

► Calibration with circular features



FILIPPO BERGAMASCO, ANDREA ALBARELLI, LUCA COSMO, EMANUELE RODOLĂĂ,
ANDREA TORSELLO

RUNE-TAG: an Accurate and Robust Artificial Marker based on Cyclic Codes

UNDER REVIEW, PAMI, 2013.

► Multi-View 3D Ellipse estimation



FILIPPO BERGAMASCO, LUCA COSMO, ANDREA ALBARELLI , ANDREA TORSELLO

A Robust Multi-Camera 3D Ellipse Fitting for Contactless Measurements

2nd Joint 3DIM/3DPVT Conference 3D Imaging, Modeling, Processing, Visualization, Transmission, IEEE, pp. 168- 175., 2012.



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Unconstrained imaging model

Introduction

Different optical setups exist demanding ad-hoc camera models

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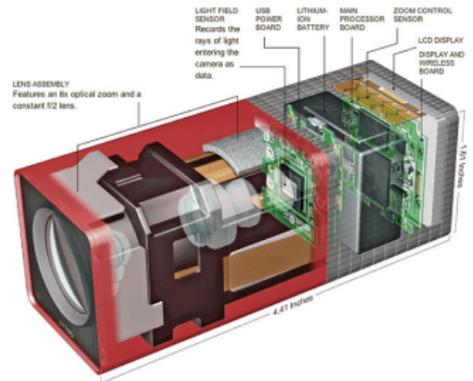
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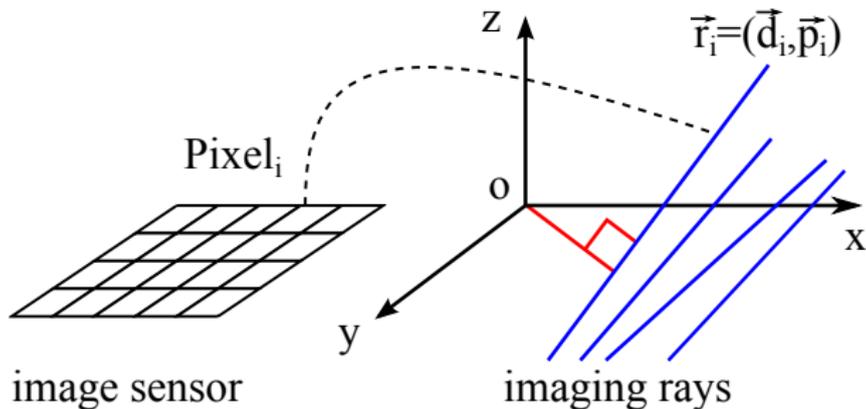
Unconstrained imaging model

Introduction

In the most general case, we can think of a

Fully-unconstrained imaging model

- ▶ Each pixel (basic light sensor) is associated to a 3D straight line (**ray**)
- ▶ Each ray is independent with respect to the others



4 dof for each ray, assuming $\vec{d}_i^T \vec{p}_i = 0$, $\|\vec{d}\| = 1$



Unconstrained imaging model

Introduction

Many advantages:

- ▶ No constraints on optical path geometry
- ▶ Can accommodate very complex lens setups

Key problem

Comprises literary millions of free parameters to estimate

- ▶ Common calibration targets fail to provide enough data
- ▶ Optimization procedure too slow
- ▶ Methods exist in literature comprising complicated calibration setups

Question:

What if we try to use such model on a quasi-pinhole camera?



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For pinhole cameras?

At first sight, it seems a nonsense! But...

- ▶ Are we sure that radial distortion can describe properly the lens inner working?
- ▶ Is the camera really pinhole?
- ▶ It would be interesting to have a single general model to describe a broad range of different cameras

Key contributions/novelty:

1. We propose an effective technique to calibrate an unconstrained camera model
2. We show that such model can achieve better results than the pinhole
3. We propose a technique to interpolate camera rays
4. We propose a variation of the method to obtain a central model with unconstrained distortion



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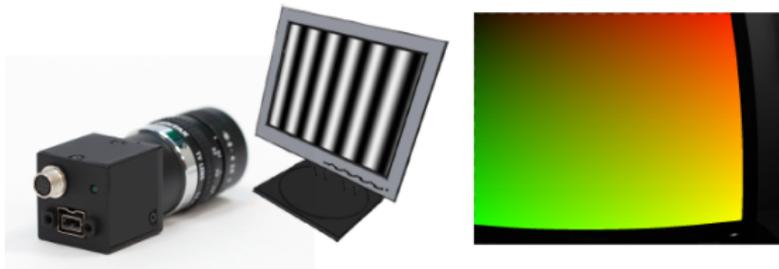
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Unconstrained imaging model Calibration

Standard point-based calibration targets simply cannot provide enough data to estimate the huge number of parameters



We solve this problem by providing a dense localization of the target obtained via structured-light patterns shown on a normal LCD display

- ▶ Phase coding with the number-theoretical phase unwrapping approach
- ▶ We encode horizontal and vertical pixel coordinates of each pixel
- ▶ High precision **sub-pixel** localization of the target coordinates of each ray



Unconstrained imaging model Calibration

Target is acquired in s different poses $\Theta_s = (R_s, \vec{t}_s)$,
 $R_s = (\vec{u}_s \vec{v}_s \vec{n}_s)$.

For each pose and ray, we have

- ▶ The observed code $\mathbf{Co}_i^s \in \mathbb{R}^2$
- ▶ The expected code

$$\mathbf{Ce}(\vec{r}_i | \Theta_s) = (\vec{u}_s \vec{v}_s)^T \left(\frac{\vec{n}_s^T (\vec{t}_s - \vec{p}_i)}{\vec{n}_s^T \vec{d}_i} \vec{d}_i + (\vec{p}_i - \vec{t}_s) \right)$$

We express the calibration process as a generalized least squares problem

$$(\hat{\vec{r}}, \hat{\Theta}) = \operatorname{argmin}_{\vec{r}, \Theta} \sum_{i,s} (\varepsilon_i^s)^T (\Sigma_i^s)^{-1} \varepsilon_i^s$$

where $\varepsilon_i^s = \mathbf{Co}_i^s - \mathbf{Ce}(\vec{r}_i | \Theta_s)$ are the code residuals and Σ_i^s is the (conditional) error covariance matrix under the given pixel-pose combination.



Unconstrained imaging model Calibration

Main Result

The generalized least squares formulation with respect to the target coordinates corresponds to the standard **linear least squares** with respect to the 3D points associated with each ray (details in the thesis).

We take advantage by the independence between rays and poses

Two step optimization process

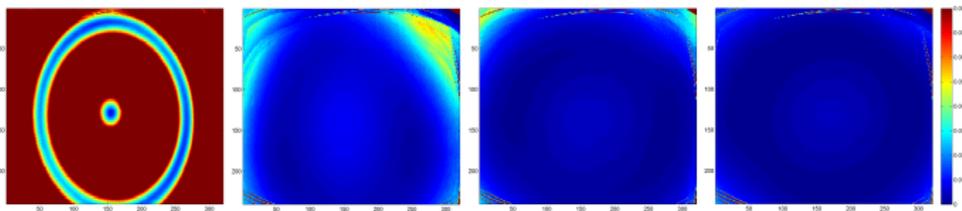
- ▶ Each ray is optimized by considering the poses fixed (lls)
- ▶ Each pose is optimized by considering the rays fixed (Point-line ICP)



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Unconstrained imaging model

Optimization results



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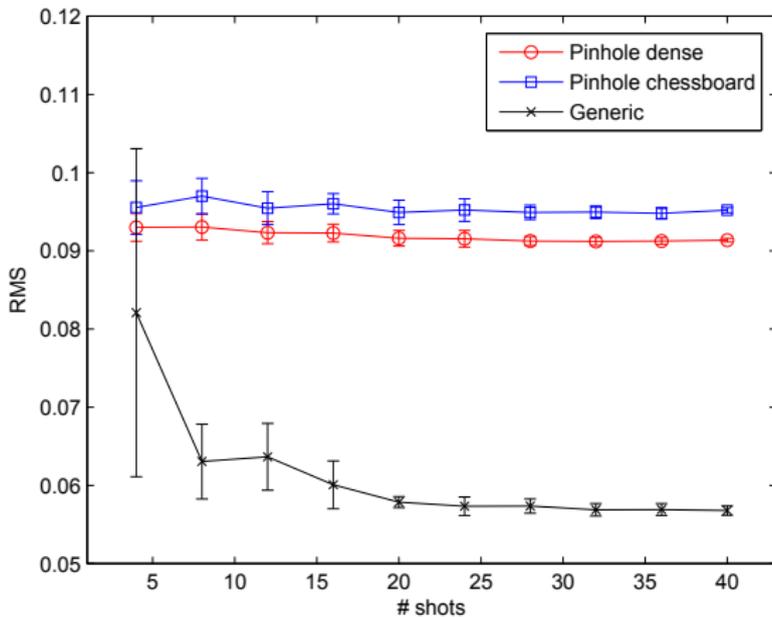
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Unconstrained imaging model

Using the model

One reason that makes pinhole model effective is that exists a continuous mapping between any point (u, v) and the corresponding ray exiting the camera.

- ▶ 3D point triangulation performed by searching correspondences
- ▶ Epipolar geometry is available
- ▶ Dense stereo, etc.

In the unconstrained model we just have a **sparse bundle of rays in space**.

Problem:

To triangulate rays and perform 3D reconstruction we need an **interpolation** function to estimate the ray associated to a given point in the image plane

- ▶ We assume some sort of smoothness in the bundle indexed by the image lattice

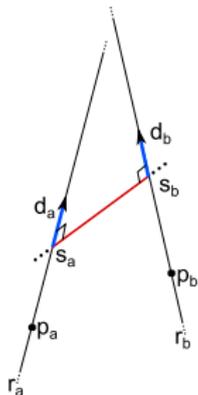


Unconstrained imaging model

Rays interpolation

Let $R_d = \{\vec{r}_i\}$ a set of n known camera rays, and $\vec{w} = (w_1, \dots, w_n) \in \mathbb{R}^n$, $\sum_{i=1}^n w_i = 1$ a convex combination of weights.

Given two rays \vec{r}_a, \vec{r}_b , we define the best rigid motion interpolant K_{ab} as the combination of:



1. The rotation R_K around the axis $\vec{d}_a \times \vec{d}_b$ with angle $\arccos(\vec{d}_a^T \vec{d}_b)$
2. The translation $T_K = \vec{s}_b - \vec{s}_a$, with \vec{s}_a and \vec{s}_b being the two rays nearest points

By describing each motion K_{ab} in terms of a screw motion represented via dual-quaternions, we pose rays interpolation in terms of **rigid motions blending**

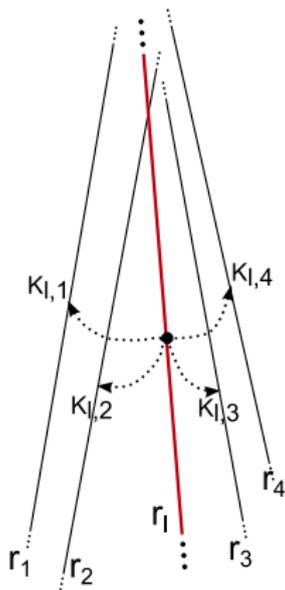


Unconstrained imaging model

Rays interpolation algorithm

Initialize the interpolated ray $\vec{r}_\ell = (\vec{d}_\ell, \vec{p}_\ell)$ as a weighted linear combination followed by a reprojection on the rays manifold:

$$\vec{d}_\ell = \frac{\sum_{i=1}^n w_i \vec{d}_i}{\|\sum_{i=1}^n w_i \vec{d}_i\|}, \vec{p}_\ell = \frac{\sum_{i=1}^n w_i \vec{p}_i}{\|\sum_{i=1}^n w_i \vec{d}_i\|} - \vec{d}_\ell \left(\vec{d}_\ell^T \frac{\sum_{i=1}^n w_i \vec{p}_i}{\|\sum_{i=1}^n w_i \vec{d}_i\|} \right)$$



1. Compute $K_{\ell,i=1\dots n}$ as the screw motion between \vec{r}_ℓ and \vec{r}_i

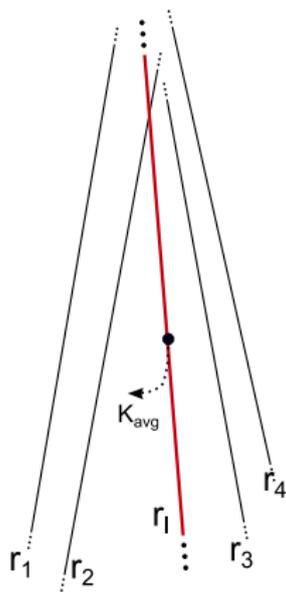


Unconstrained imaging model

Rays interpolation algorithm

Initialize the interpolated ray $\vec{r}_\ell = (\vec{d}_\ell, \vec{p}_\ell)$ as a weighted linear combination followed by a reprojection on the rays manifold:

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1. Compute $K_{\ell, i=1 \dots n}$ as the screw motion between \vec{r}_ℓ and \vec{r}_i
2. Perform *Dual-quaternion Iterative Blending* algorithm to obtain K_{avg}

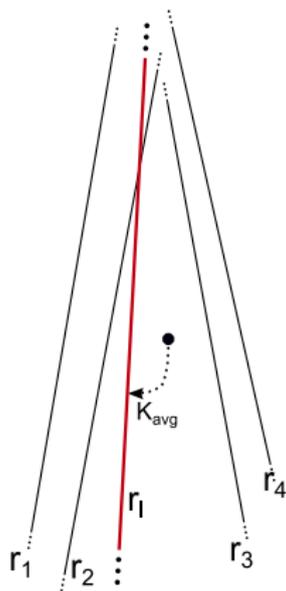


Unconstrained imaging model

Rays interpolation algorithm

Initialize the interpolated ray $\vec{r}_\ell = (\vec{d}_\ell, \vec{p}_\ell)$ as a weighted linear combination followed by a reprojection on the rays manifold:

$$\vec{d}_\ell = \frac{\sum_{i=1}^n w_i \vec{d}_i}{\|\sum_{i=1}^n w_i \vec{d}_i\|}, \vec{p}_\ell = \frac{\sum_{i=1}^n w_i \vec{p}_i}{\|\sum_{i=1}^n w_i \vec{d}_i\|} - \vec{d}_\ell \left(\vec{d}_\ell^T \frac{\sum_{i=1}^n w_i \vec{p}_i}{\|\sum_{i=1}^n w_i \vec{d}_i\|} \right)$$



1. Compute $K_{\ell, i=1 \dots n}$ as the screw motion between \vec{r}_ℓ and \vec{r}_i
2. Perform *Dual-quaternion Iterative Blending* algorithm to obtain K_{avg}
3. Apply K_{avg} to \vec{r}_ℓ
4. Return to step 1 and iterate until convergence

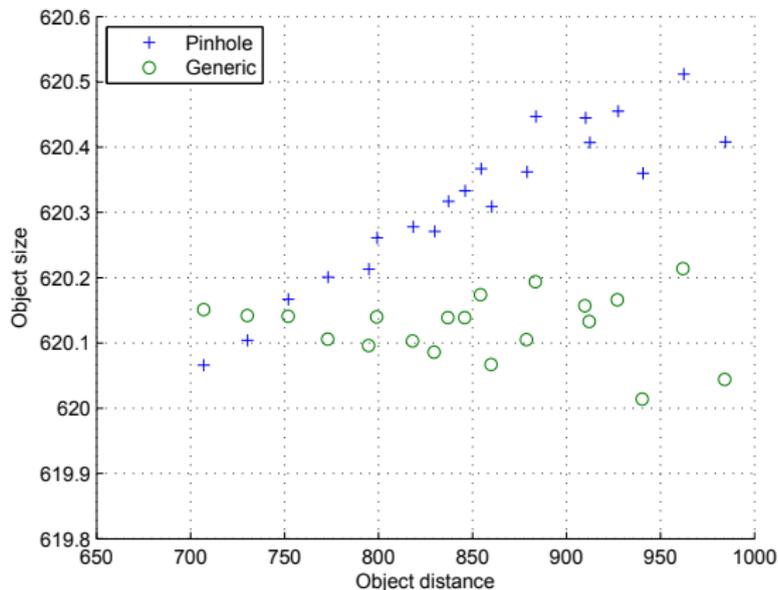


Unconstrained imaging model

Stereo triangulation experiment

We tested the performance of the unconstrained model for stereo triangulation.

- ▶ Stereo *RT* computed via the same point-rays ICP
- ▶ As interpolation weights we used the inverse of the squared distances of 8 neighbours





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Introduction

- ▶ We demonstrated the effectiveness of the unconstrained model even for quasi pinhole cameras
- ▶ Many classical computer vision techniques heavily rely on the epipolar geometry given by central projection
- ▶ We believe that most of the improvements exhibited by the unconstrained model are due to a better **lens distortion** accommodation

Proposed tradeoff:

Fall-back to a **central** model but allowing a complete **unconstrained distortion**



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Calibration process

The calibration process starts from estimate the bundle of camera rays

- ▶ Alternating optimization of rays assuming fixed poses, viceversa
- ▶ Pose estimation step exactly as before
- ▶ Rays optimization step slightly more complicated as it must estimate the common optical center o

Since rays are all forced to pass trough o , they are parametrized just by a vector $d_i \in \mathbb{R}^3$, $\|d\| = 1$

$$(\hat{\vec{d}}, \hat{\Theta}, \hat{o}) = \underset{\vec{d}, o, \Theta}{\operatorname{argmin}} \sum_{i,s} (\varepsilon_i^s)^T (\Sigma_i^s)^{-1} \varepsilon_i^s$$



Pinhole model with unconstrained distortion

Rays and optical center calibration step

Let $\mathbf{x}_{(u,v)}^s = RT_s \left(\mathbf{Co}_{(u,v)}^s \quad 0 \quad 1 \right)^T$ be the 3D coordinates of the observed code $\mathbf{Co}_{(u,v)}^s$ transformed through the pose RT_s .

We can formulate the estimation of o as:

$$\operatorname{argmin}_o \sum_{u,v} \min_{d_{(u,v)}} \sum_s \left\| (h_{(u,v)}^s)^T (I - d_{(u,v)} d_{(u,v)}^T) \right\|^2$$

Where $h_{(u,v)}^s = (\mathbf{x}_{(u,v)}^s - o)$.

Key result

Under the assumption that the distance between each ray and its expected code is small, this can be transformed in term of the **point clouds** generated by the intersection of a ray and each target pose



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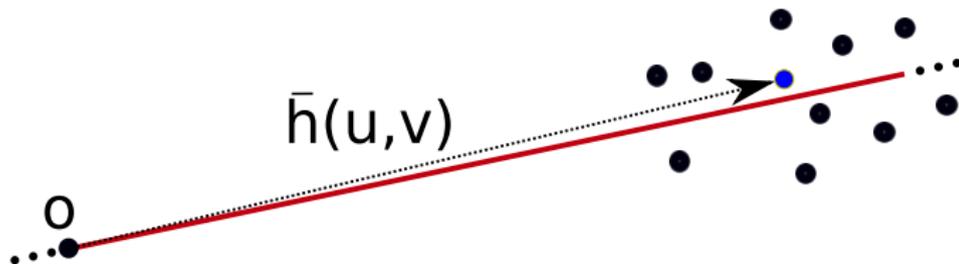
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Rays and optical center calibration step



$$\operatorname{argmax}_o \sum_{u,v} N_{(u,v)} \frac{\bar{h}_{(u,v)}^T \mathbf{S}_{(u,v)} \bar{h}_{(u,v)}}{\|\bar{h}_{(u,v)}\|^2}$$

- ▶ $\mathbf{S}_{(u,v)}$ Covariance of the point cloud
- ▶ $N_{(u,v)}$ number of points in the cloud
- ▶ $\bar{h}_{(u,v)}$ is the vector connecting o and the cloud centroid

The functional is further rewritten to be solved as a fixed point iteration



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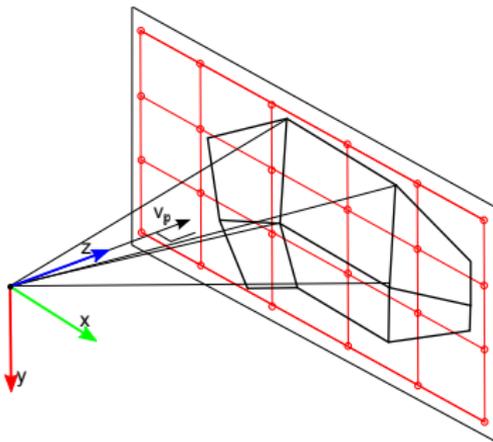
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Pinhole model with unconstrained distortion

Estimating a new virtual pinhole

After ray bundle recovery we create a **virtual pinhole camera**. We need to estimate:

- ▶ Image plane orientation and distance
- ▶ The undistortion mapping to obtain a regular grid



- ▶ plane orientation minimizing the variance of distances between each plane-ray intersection point
- ▶ points topology inherited by image lattice
- ▶ points resampled in a uniform grid to compute the undistortion function
- ▶ value at each grid point as function of 4 neigh.



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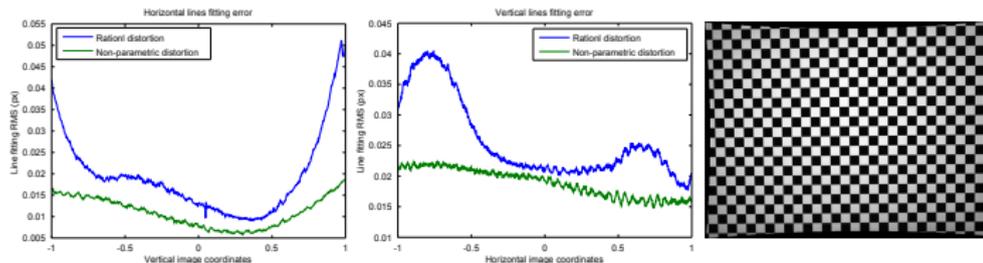
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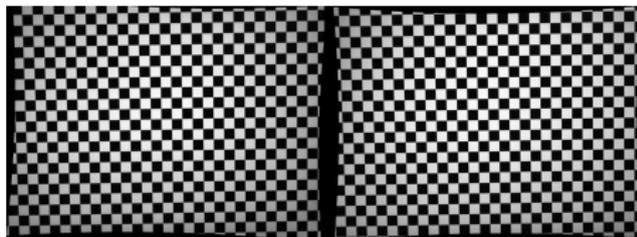
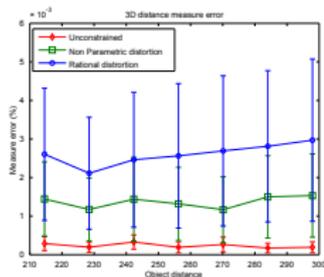
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Better radial distortion correction:



An unified model for mono and stereo cameras

Stereo cameras can be seen as a unique bundle of rays
with an undistortion function that rectifies epipolar lines





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Better and fast 3D reconstruction through dense stereo

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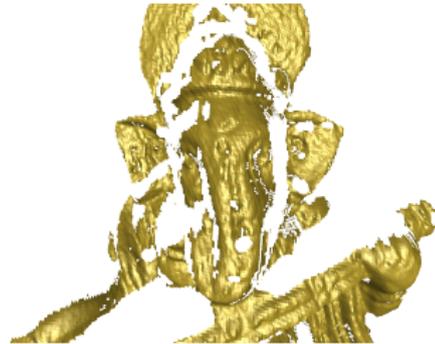
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OpenCV Undistort+Rectify



Proposed method



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Conclusions

- ▶ We proposed an effective calibration technique for a fully unconstrained camera model
- ▶ We demonstrated its advantages even for quasi pinhole cameras
- ▶ We proposed a method to create virtual pinhole cameras with model-free distortion functions
 - ▶ Very effective also for stereo rigs



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Simultaneous Optical Flow and Dichromatic Parameters Recovery



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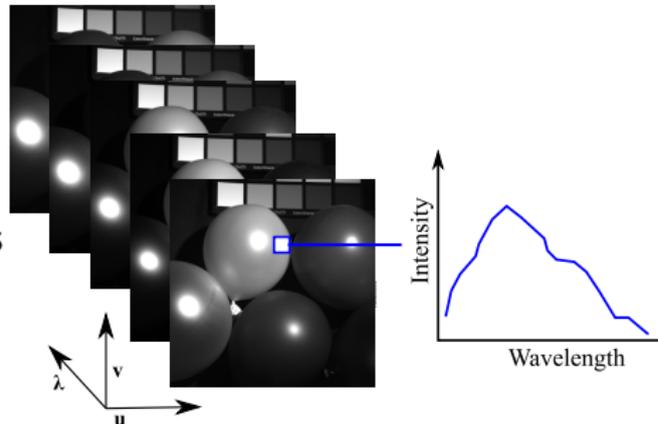
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Flow and Dichromatic parameters recovery

Introduction

- ▶ We usually see cameras as a grid of simple photons collectors disposed in a grid.
- ▶ When we start discriminating on light frequency, we enter the field of Multi-Spectral imaging
- ▶ RGB camera is a multi-spectral device with just 3 bands

- ▶ Data cube representation
- ▶ Multi-spectral data leverage the analysis to physical properties of materials





Flow and Dichromatic parameters recovery

Introduction

We assume a uniform illuminant spectrum

Dichromatic Model

Expresses the image radiance $I(\mathbf{u}, \lambda)$ at pixel location $\mathbf{u} = (u_1, u_2)$ and wavelength λ as:

$$I(\mathbf{u}, \lambda) = g(\mathbf{u})L(\lambda)S(\mathbf{u}, \lambda) + k(\mathbf{u})L(\lambda)$$

- ▶ I is the “cube” measured by the camera
- ▶ g is the shading. Depends by **geometry**
- ▶ S is the reflectance. Depends by **material**
- ▶ L is the illuminant
- ▶ k is a specular factor



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In literature there exist different approaches to factorize S , L , g and k given a single radiance image I .

Reflectance is particularly interesting being invariant to the object geometry and its relative position wrt. the viewer

- ▶ Is preserved across **multiple images** of the scene

Novelties of the proposed approach

1. The first two-views dichromatic model recovery method
2. We developed a novel affine hyper-prior combined with a TV regularizer



Flow and Dichromatic parameters recovery

Problem formulation

Two input irradiance images of the same scene are given:

$$I_1(\mathbf{u}, \lambda), I_2(\mathbf{u}, \lambda)$$

An optical flow function $f(\mathbf{u}) = \mathbf{u}' : \Omega_1 \rightarrow \Omega_2$ maps points from the first to the second image

The “constant brightness assumption” is not valid for highly specular pixels

- ▶ Brightness strongly dependent on the relative angle between the observer and the light

We make use of the multiplicative gating function

$$W(\mathbf{u}) = \exp(-\tau \|I(\mathbf{u}, \lambda) - \mathcal{P}(I(\mathbf{u}, \lambda))\|)$$

where $\mathcal{P}(I(\mathbf{u}, \lambda))$ is the projection of the image radiance $I(\mathbf{u}, \lambda)$ onto the dichromatic plane.



Flow and Dichromatic parameters recovery

Problem formulation

We defined two energy terms measuring the coherency of the recovered dichromatic model and flow with the input data

$$E_{DI_1} = \int_{\Omega_1} W_1(\mathbf{u})^2 \sum_{\lambda} \left(I_1(\mathbf{u}, \lambda) - L(\lambda) \left(g_1(\mathbf{u}) S(\mathbf{u}, \lambda) + k_1(\mathbf{u}) \right) \right)^2 d\mathbf{u}$$

$$E_{DI_2} = \int_{\Omega_1} W_2(\mathbf{u}')^2 \sum_{\lambda} \left(I_2(\mathbf{u}', \lambda) - L(\lambda) \left(g_2(\mathbf{u}') S(\mathbf{u}, \lambda) + k_2(\mathbf{u}') \right) \right)^2 d\mathbf{u}$$

Note

Due to the gating functions, the evaluation is performed only on non specular areas. Hence, the contribution of k_1 and k_2 is negligible



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Problem formulation

We pose the problem as the minimization of the energy functional:

$$\operatorname{argmin}_{f, S, L, g} (\mu E_{DI_1} + (1 - \mu) E_{DI_2})$$

The problem is highly under-determined. The flow function itself allows many different solutions.

A common approach is to use a regularizer enforcing a certain degree of smoothness in the solution

- ▶ Many different regularizers proposed over the last decades
- ▶ Aim: Preserve edges, possibly implying physical/meaningful constraints



Flow and Dichromatic parameters recovery

Total Variation regularizer

Let f be a differentiable function. The Total Variation (TV) of f is defined as:

$$\text{TV}(f) = \int_{\Omega} \|Df(x)\|_2 dx$$

Main property

Used as a regularizer, TV privileges piecewise constant solutions.

Unfortunately, the regularized optimization problem

$$\min_f E(f) + \text{TV}(f)$$

is not convex. We switch to the relaxed problem:

$$\min_{f, f_{\text{TV}}} E(f) + \int \frac{\|f - f_{\text{TV}}\|^2}{\delta} + \text{TV}(f_{\text{TV}})$$



Flow and Dichromatic parameters recovery

Optical Flow parametrization

Using a TV regularizer is a natural choice for S

- ▶ We expect large areas of the same material

However, it does not make sense to impose piecewise constant flow parametrized as displacements on the image plane

Key contribution

We use a higher order smoothness prior, where the displacement is assumed to be locally affine:

$$f(\mathbf{u}) = \mathbf{u} + A(\mathbf{u})\mathbf{u} = \begin{pmatrix} u \\ v \\ 1 \end{pmatrix} + \begin{pmatrix} a_1(\mathbf{u}) & a_2(\mathbf{u}) & a_3(\mathbf{u}) \\ a_4(\mathbf{u}) & a_5(\mathbf{u}) & a_6(\mathbf{u}) \\ 0 & 0 & 0 \end{pmatrix} \begin{pmatrix} u \\ v \\ 1 \end{pmatrix}$$

Approximates view transformation under a weak camera model of **local planar patches**.



Flow and Dichromatic parameters recovery Optimization

$$E = \alpha (\mu E_{DI_1} + (1 - \mu) E_{DI_2}) + \rho_S \left(\int_{\Omega_1} \frac{\|S(\mathbf{u}) - S_{TV}(\mathbf{u})\|_2^2}{\delta_S} d\mathbf{u} + \int_{\Omega_1} \|DS_{TV}(\mathbf{u})\|_2 d\mathbf{u} \right) \quad (1)$$

$$+ \rho_f \left(\int_{\Omega_1} \frac{\|A(\mathbf{u}) - A_{TV}(\mathbf{u})\|_2^2}{\delta_f} d\mathbf{u} + \int_{\Omega_1} \|DA_{TV}(\mathbf{u})\|_2 d\mathbf{u} \right) \quad (2)$$

which is minimized over S , f , L , g_1 , g_2 , S_{TV} , and f_{TV} .

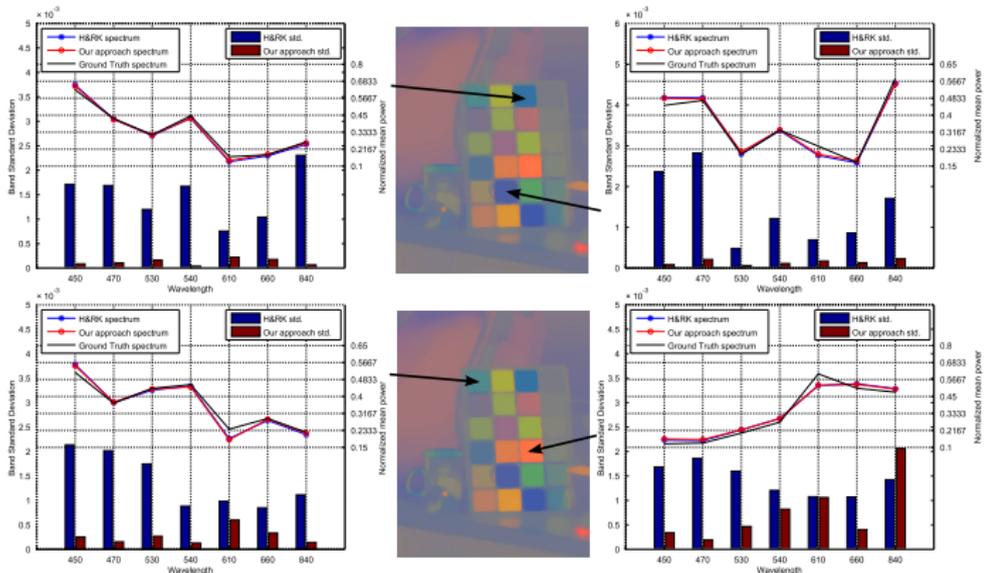
Alternating minimization

1. Minimize with respect to $L(\lambda)$, $g_1(\mathbf{u})$, and $g_2(f(\mathbf{u}))$, keeping $S(\mathbf{u}, \lambda)$, $f(\mathbf{u})$, $S_{TV}(\mathbf{u}, \lambda)$ and $A_{TV}(\mathbf{u})$ fixed;
2. Update $S(\mathbf{u}, \lambda)$ and $f(\mathbf{u})$ through a gradient descent step, keeping all other variables fixed;
3. Minimize (1) and (2) to obtain a new estimate of $A_{TV}(\mathbf{u})$ and $S_{TV}(\mathbf{u})$.

Flow and Dichromatic parameters recovery

Results

- ▶ For our tests we used a multi-spectral device delivering 6 channels in visible spectrum and one in the near-infrared
- ▶ We compare with the current industrial-grade state-of-the-art



Our approach shows less std. and better reflectance recovery



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Flow and Dichromatic parameters recovery

Qualitative Results



Input

Reflectance

Unconstrained
Imaging Model

Calibration

Rays interpolation

Central + Model-free
distortion

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Problem formulation

TV regularizer

> Results



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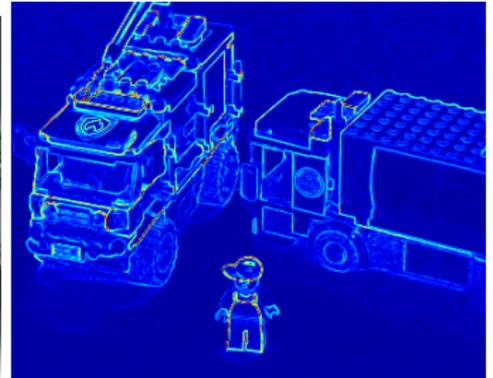
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Input

Reflectance norm



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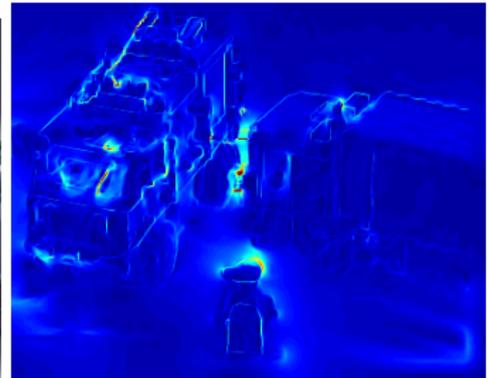
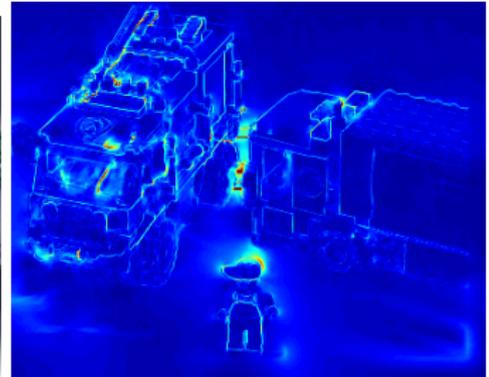
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Flow and Dichromatic parameters recovery

Qualitative Results



Input

Flow norm



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Conclusions

- ▶ We proposed a novel technique to simultaneously recover the optical flow and dichromatic parameters from two-views
- ▶ Our method encompass the current state-of-the-art delivering a better factorization of dichromatic components
- ▶ The novel affine hyper-prior combined with a TV regularizer provides a natural piecewise-rigid assumption on the motion under a weak camera model
- ▶ The TV regularized for reflectance impose local patches of uniform material
- ▶ We are currently working on a novel homographic hyper-prior



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Thank you for your attention
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